

$\alpha$	$\frac{\pi}{6} = 30^\circ$	$\frac{\pi}{4} = 45^\circ$	$\frac{\pi}{3} = 60^\circ$
$\sin \alpha$	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$
$\cos \alpha$	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$
$\tan \alpha$	$\frac{\sqrt{3}}{3}$	1	$\sqrt{3}$
$\cot \alpha$	$\sqrt{3}$	1	$\frac{\sqrt{3}}{3}$

### The most commonly used quadrantal angles

$\alpha$	$\sin \alpha$	$\cos \alpha$	$\tan \alpha$	$\cot \alpha$
0	0	1	0	$\times$
$\frac{\pi}{2}$	1	0	$\times$	0
$\pi$	0	-1	0	$\times$
$\frac{3}{2}\pi$	-1	0	$\times$	0
$2\pi$	0	1	0	$\times$

### Trigonometric identities

$$\tan \alpha = \frac{\sin \alpha}{\cos \alpha}$$

$$\cot \alpha = \frac{\cos \alpha}{\sin \alpha}$$

$$\tan \alpha \cdot \cot \alpha = 1$$

$$\sin^2 \alpha + \cos^2 \alpha = 1$$

$$\sin(2\alpha) = 2 \sin \alpha \cos \alpha$$

$$\cos(2\alpha) = \cos^2 \alpha - \sin^2 \alpha$$

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$$

### Properties of exponents

If  $a, b > 0$  and  $x, y \in R$ ,

- $a^{x+y} = a^x a^y$

- $a^{x-y} = \frac{a^x}{a^y}$

- $(a^x)^y = a^{xy}$

- $(ab)^x = a^x b^x$

- $a^{-x} = \frac{1}{a^x}$

### Root rules

If  $a \geq 0, b \geq 0, m, n \in N \setminus \{0\}$  then

- $\sqrt[n]{a \cdot b} = \sqrt[n]{a} \cdot \sqrt[n]{b}$ ,

- $\sqrt[n]{\frac{a}{b}} = \frac{\sqrt[n]{a}}{\sqrt[n]{b}}, (b \neq 0)$ ,

- $\sqrt[n]{\sqrt[m]{a}} = \sqrt[n \cdot m]{a} = \sqrt[m]{\sqrt[n]{a}}$ ,

- $a^{\frac{m}{n}} = \sqrt[n]{a^m}$

- $a^{-\frac{m}{n}} = \frac{1}{\sqrt[n]{a^m}}$

### Properties of logs

If  $a, b > 0, a, b \neq 1$  and  $x, y > 0$

- $\log_a 1 = 0$

- $\log_a a = 1$

- $\log_a a^x = x$

- $a^{\log_a x} = x$

- $\log_a x = \frac{\log_b x}{\log_b a}$

- $\log_b a = \frac{1}{\log_a b}$

- $\log_a (xy) = \log_a x + \log_a y$

- $\log_a \left(\frac{x}{y}\right) = \log_a x - \log_a y$

- $\log_a x^n = n \log_a x$